

## CS 454: Theory of Computation

### Problem Solving Session #01

## Questions

Design the following DFAs

- Q1. Alphabet  $\Sigma = \{0, 1\}$ . Accepts strings with odd number of 1's.
- Q2. Alphabet  $\Sigma = \{a, b, c\}$ . Accepts strings that include  $aab$  as a substring.
- Q3. Alphabet  $\Sigma = \{a, b\}$ . Accepts any strings that include  $aababba$  as a substring.
- Q4. Alphabet  $\Sigma = \{a, b, /, *\}$ . Accepts strings inside C-style comments. e.g. accepts  $/* abab */$  but rejects  $ab */$ .
- Q5. \* Alphabet  $\Sigma = \{a, b, /, *\}$ . Accepts strings that are not inside C-style comments.
- Q6. Alphabet  $\Sigma = \{0, 1\}$ . Accepts any strings with two consecutive zeros.
- Q7. Alphabet  $\Sigma = \{0, 1\}$ . Accepts all strings that start with 00.
- Q8. Alphabet  $\Sigma = \{a, b\}$ . Accepts all strings where  $as$  and  $bs$  alternate.
- Q9. Alphabet  $\Sigma = \{a, b\}$ . Accepts all strings that start and end with the same symbol, i.e.,  
 $L = \{w \mid w \in \Sigma^*, w = a\{a, b\}^*a \cup b\{a, b\}^*b\}$ .
- Q10. Alphabet  $\Sigma = \{a, b\}$ . Accepts strings that have at least one  $a$  and exactly 2  $bs$ .
- Q11. Alphabet  $\Sigma = \{a, b\}$ . Accepts the language  $L = \{w \mid |w| \bmod 3 = 0\}$ .
- Q12. Alphabet  $\Sigma = \{a, b\}$ . Show that the language  $L = \{v w v \mid v, w \in \Sigma^*, |v| = 2\}$ .